

SIMILARITY

SIMILARITY (definition): Two objects are *similar* if they have the same shape, but they do not have to have the same size. The objects must be proportional: one object can be scaled (enlarged or reduced), possibly with additional translation, rotation, and reflection, to be the exactly the same as the other object. This means that either object can be rescaled and repositioned (and possibly reflected), so as to coincide precisely with the other object.

Properties of Similar Figures	
Corresponding angles of similar figures are congruent.	
Corresponding sides of similar figures are proportional.	
If $\triangle ABC \sim \triangle XYZ$, then	
$\angle A \cong \angle X \quad \angle B \cong \angle Y \quad \angle C \cong \angle Z$ $\frac{AB}{XY} = \frac{BC}{YZ} = \frac{AC}{XZ}$	

SIMILARITY STATEMENT: When two objects are similar, we can write a similarity statement. In the above example, the similarity statement is:

$$\triangle ABC \sim \triangle XYZ.$$

The order of the *vertices* (angles represented by letters) in the similarity statement is very important. The statement $\triangle ABC \sim \triangle XYZ$ indicates that:

$$\begin{aligned} \angle A &\text{ corresponds to } \angle X, \\ \angle B &\text{ corresponds to } \angle Y, \\ \angle C &\text{ corresponds to } \angle Z. \end{aligned}$$

The reason the order is so important is that with any set of similar objects, the corresponding angles are congruent, meaning they have the exact same measure. In the above example:

$$\angle A \cong \angle X \quad \angle B \cong \angle Y \quad \angle C \cong \angle Z$$

The order of the vertices also indicate with sides are proportional, meaning they have the exact same ratio. We normally put the smaller length over the larger length when determining proportionality. In the above example:

$$\frac{AB}{XY} \cong \frac{BC}{YZ} \cong \frac{AC}{XZ}$$

Only if the vertices are congruent and the sides are proportional, are the objects similar. If one is not congruent or proportional, the objects are not similar.

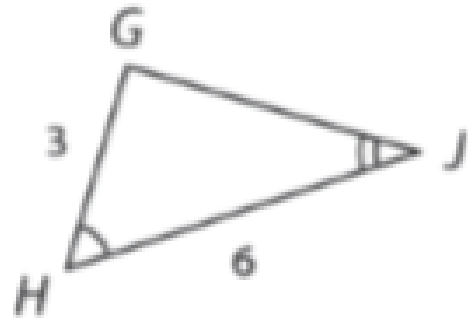
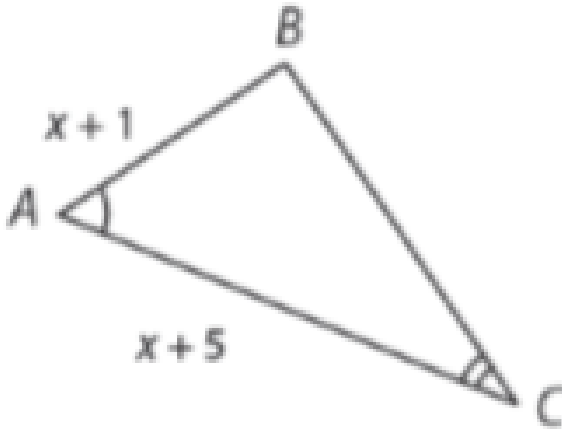
TRIANGLE SIMILARITY

SIMILARITY POSTULATES: There are three postulates we can use to prove that two *triangles* are similar.

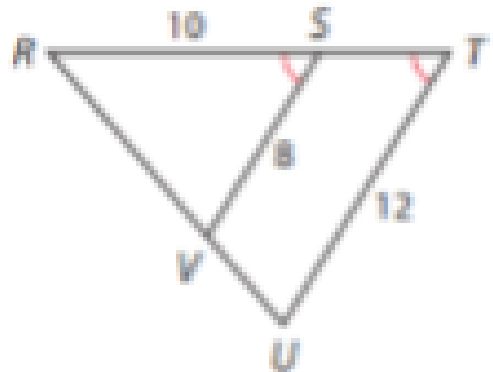
1. **ANGLE-ANGLE (AA):** If two angles of one triangle are congruent to two angles of another triangle, then the two triangles are similar.
2. **SIDE-SIDE-SIDE (SSS):** If all three sides of one triangle are proportional to the corresponding sides of another triangle, then the triangles are similar.
3. **SIDE-ANGLE-SIDE (SAS):** If two sides of one triangle are proportional to the corresponding sides of another triangle **and** the included angles are congruent, the triangles are similar.

PRACTICE

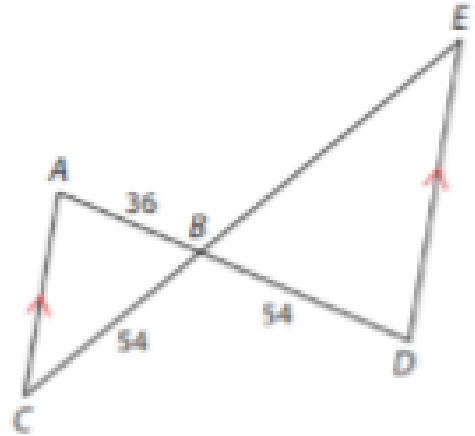
1. Given: $\triangle ABC \sim \triangle HGJ$. Find x .



2. Given: $\triangle RSV \sim \triangle RTU$. Find RT .



3. Given: $\triangle ABC \sim \triangle DBE$. Find BE .

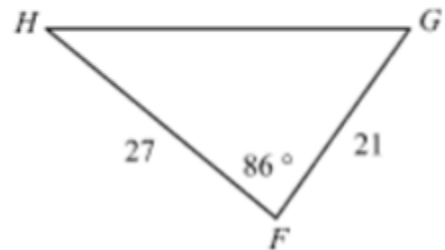


- In the following questions:
- 1) State if the triangle are similar;
 - 2) If they are similar, by what similarity theorem can it be proven (AA, SSS, SAS);
 - 3) If they are similar, finish the similarity statement.

4. Are the triangles similar?

If yes, by what theorem?

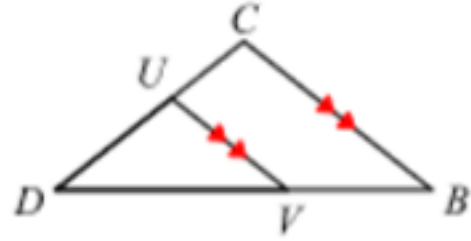
If yes: $\triangle FGH \sim$ _____



5. Are the triangles similar?

If yes, by what theorem?

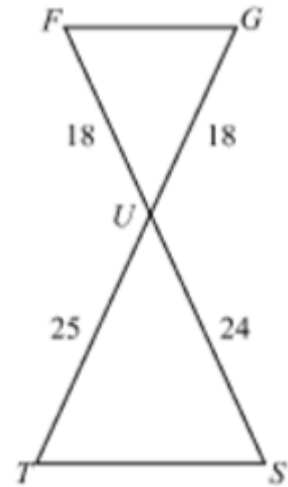
If yes: $\triangle DCB \sim$ _____



6. Are the triangles similar?

If yes, by what theorem?

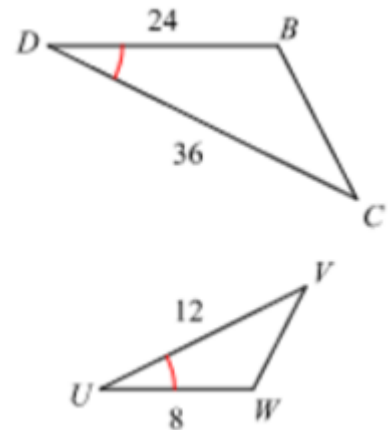
If yes: $\triangle UTS \sim$ _____



7. Are the triangles similar?

If yes, by what theorem?

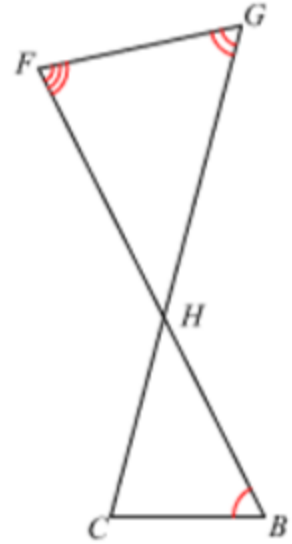
If yes: $\triangle DCB \sim$ _____



8. Are the triangles similar?

If yes, by what theorem?

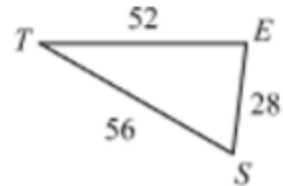
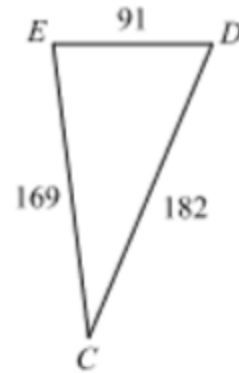
If yes: $\triangle HGF \sim$ _____



9. Are the triangles similar?

If yes, by what theorem?

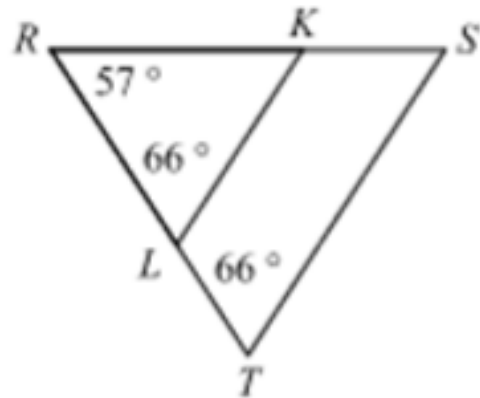
If yes: $\triangle EDC \sim$ _____



10. Are the triangles similar?

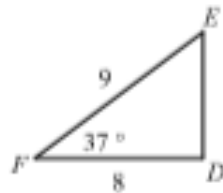
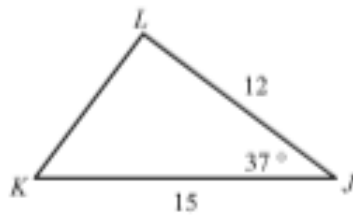
If yes, by what theorem?

If yes: $\triangle RST \sim$ _____



State if the triangles in each pair are similar. If so, state how you know they are similar and complete the similarity statement.

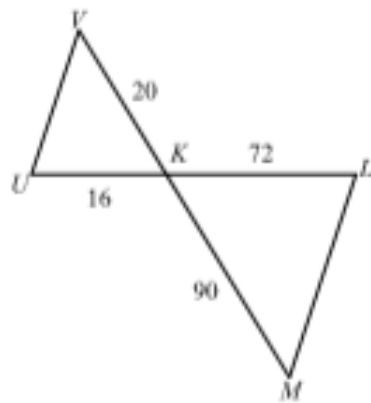
1)



$\triangle JKL \sim$ _____

- A) similar; AA similarity; $\triangle DEF$
- B) not similar
- C) similar; SSS similarity; $\triangle EDF$
- D) similar; SAS similarity; $\triangle EDF$

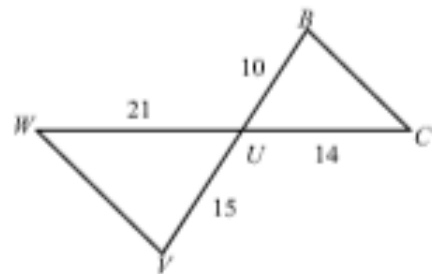
3)



$\triangle KLM \sim$ _____

- A) not similar
- B) similar; SAS similarity; $\triangle KUV$
- C) similar; SAS similarity; $\triangle UVK$
- D) similar; AA similarity; $\triangle KVU$

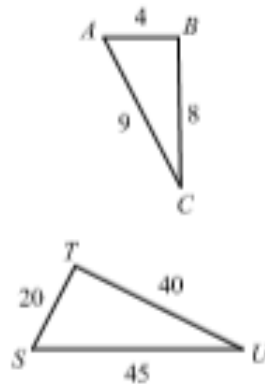
2)



$\triangle UVW \sim$ _____

- A) similar; SSS similarity; $\triangle UBC$
- B) not similar
- C) similar; SSS similarity; $\triangle BUC$
- D) similar; SAS similarity; $\triangle UBC$

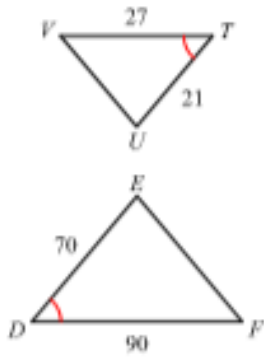
4)



$\triangle STU \sim$ _____

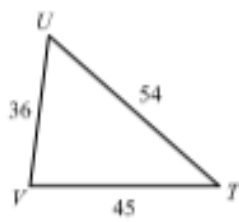
- A) similar; SSS similarity; $\triangle ABC$
- B) similar; AA similarity; $\triangle ACB$
- C) similar; AA similarity; $\triangle ABC$
- D) not similar

7)



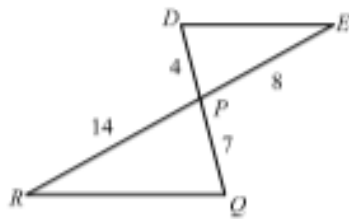
$\Delta DEF \sim$ _____

9)



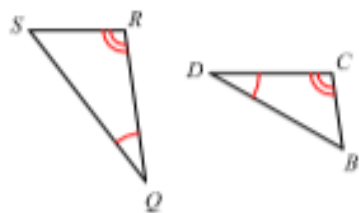
$\Delta VUT \sim$ _____

11)



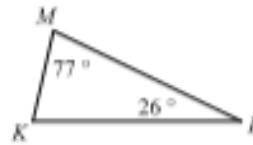
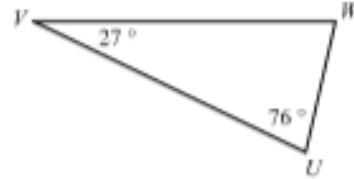
$\Delta PQR \sim$ _____

13)



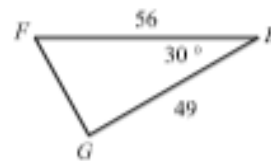
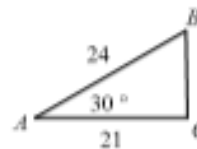
$\Delta QRS \sim$ _____

8)



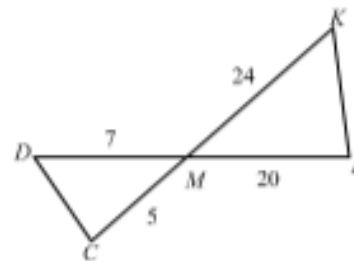
$\Delta UVW \sim$ _____

10)



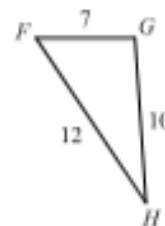
$\Delta EFG \sim$ _____

12)



$\Delta MLK \sim$ _____

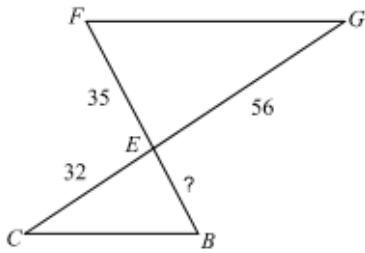
14)



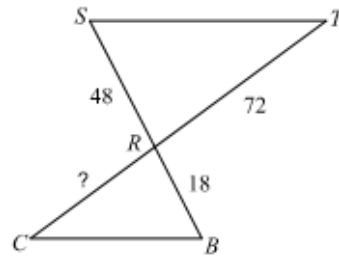
$\Delta HGF \sim$ _____

Find the missing length. The triangles in each pair are similar.

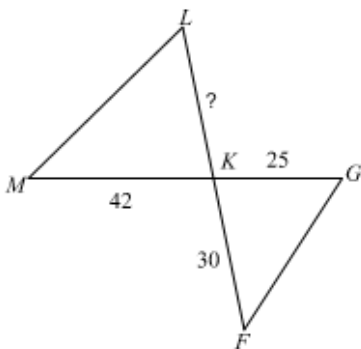
1) $\triangle EFG \sim \triangle EBC$



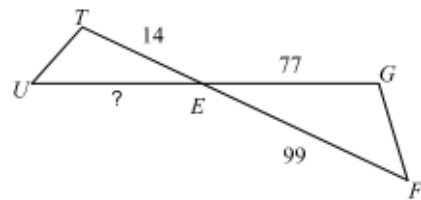
2) $\triangle RST \sim \triangle RBC$



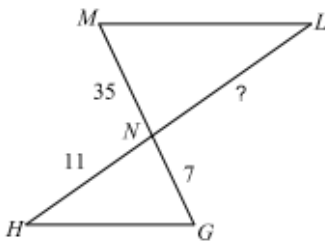
3) $\triangle KLM \sim \triangle KGF$



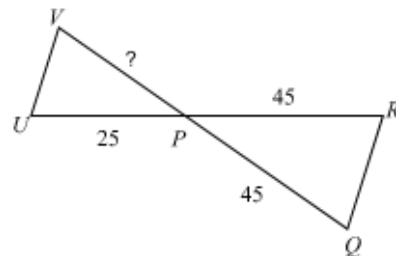
4) $\triangle EFG \sim \triangle EUT$



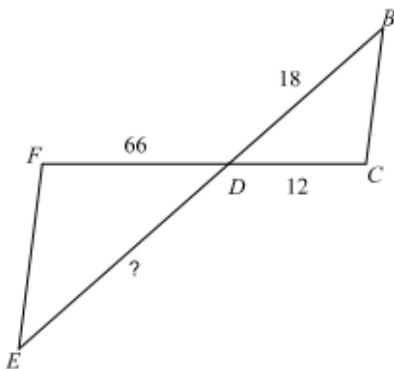
5) $\triangle NML \sim \triangle NGH$



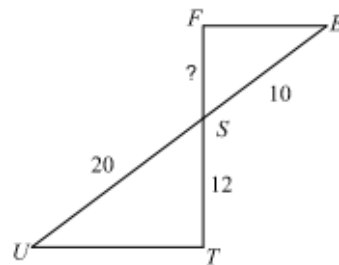
6) $\triangle PQR \sim \triangle PUV$



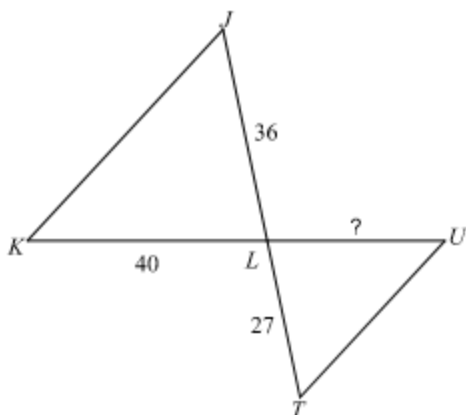
7) $\triangle DEF \sim \triangle DBC$



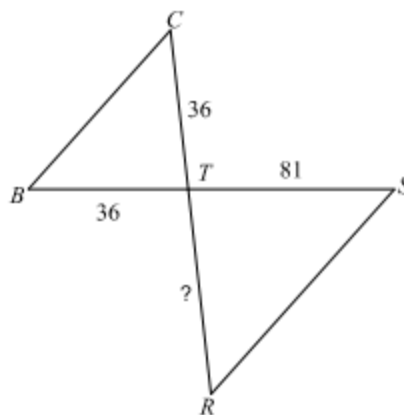
8) $\triangle STU \sim \triangle SFE$



9) $\triangle LKJ \sim \triangle LUT$

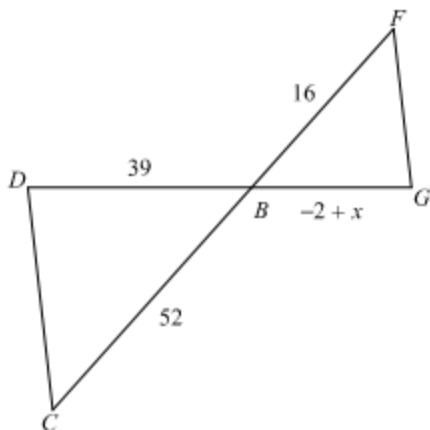


10) $\triangle TSR \sim \triangle TBC$

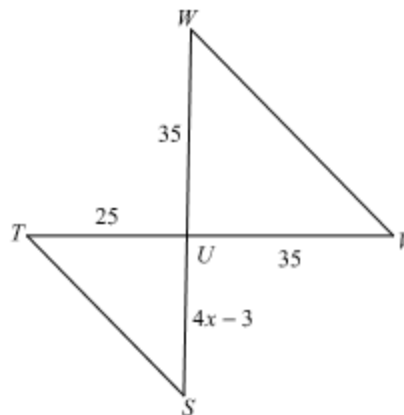


Solve for x . The triangles in each pair are similar.

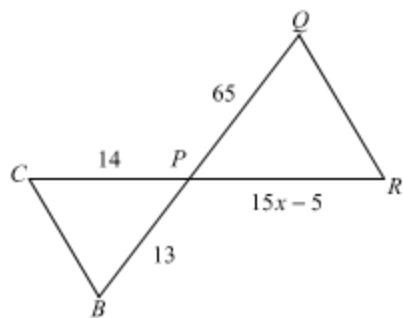
11) $\triangle BCD \sim \triangle BFG$



12) $\triangle UVW \sim \triangle UST$



13) $\triangle PQR \sim \triangle PBC$



14) $\triangle TUV \sim \triangle TRQ$

